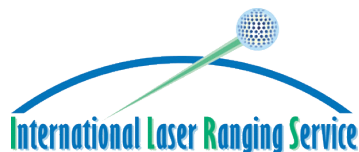


# Consistent estimation of Earth rotation, geometry and gravity with DGFI's multi-satellite SLR solution

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# GGOS aims

## Geometry

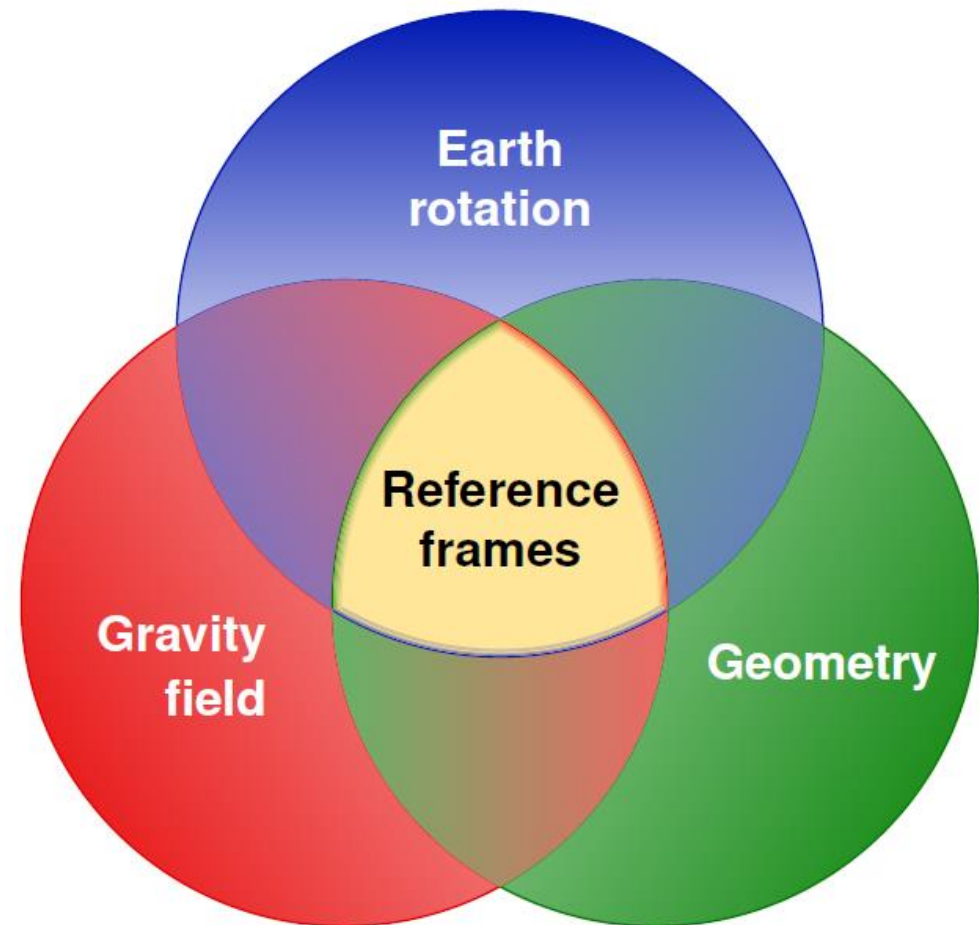
- measuring the geometric shape of the Earth's surface and its kinematics & variations

## Earth rotation

- monitoring the variations of the Earth's rotation as indicator of angular momentum and torques

## Gravity field

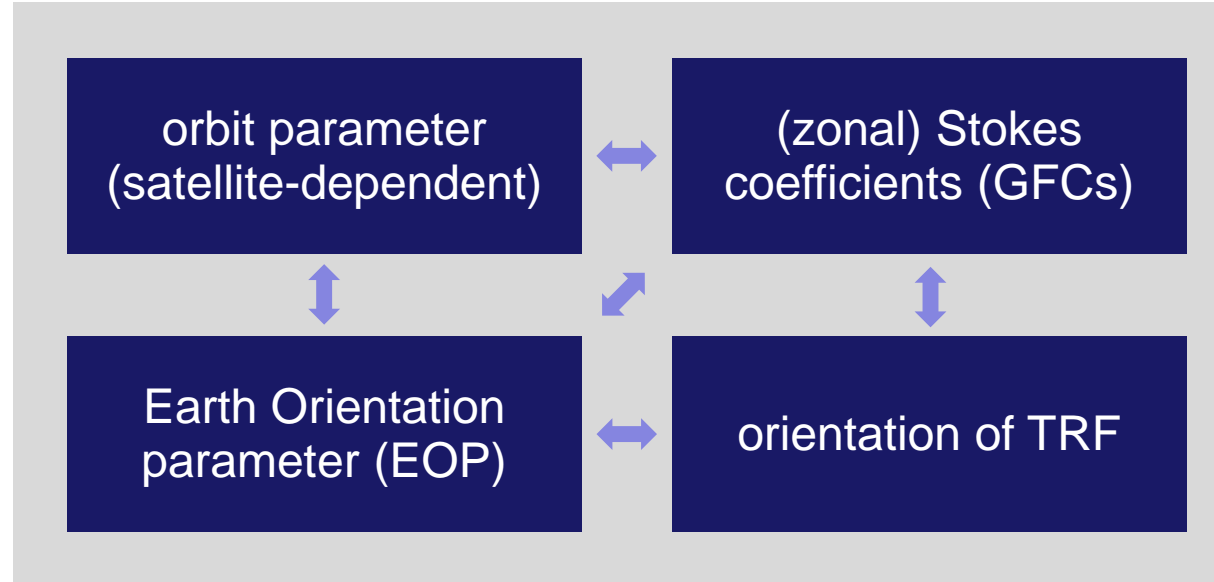
- determining and monitoring the Earth's gravity field
- Highly-accurate and consistent **reference frames** are required to integrate the three pillars.



[acc. to Plag & Pearlman, 2009]

# Interaction between the “pillars”

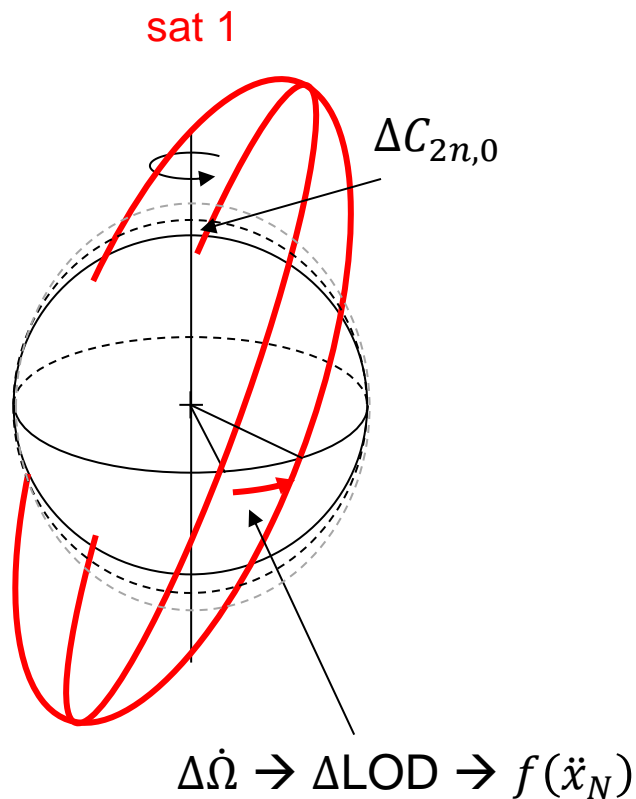
- **GGOS goal:** Consistent estimation of the Earth’s geometry, the Earth’s orientation and the Earth’s gravity field and its temporal variations
- **problem:** High interaction between different parameter groups in a common adjustment (also complementary parameters!)



- **inter-technique solution:** Combination of observation techniques with different advantages (e.g. GNSS, SLR, VLBI, DORIS, GRACE, GOCE, ...)
- **intra-technique solution:** Combination of SLR observations to satellites with different orbit characteristics

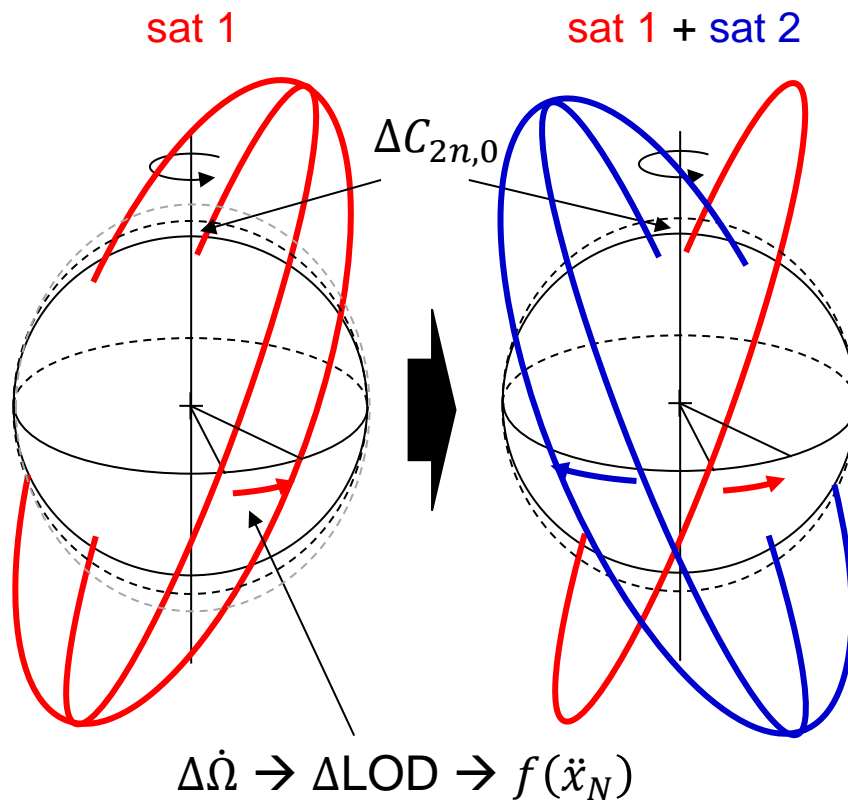
# Correlations I

- **sat 1**: high correlations between Earth gravity field, nodal precession, empirical cross-track accelerations and Earth rotation



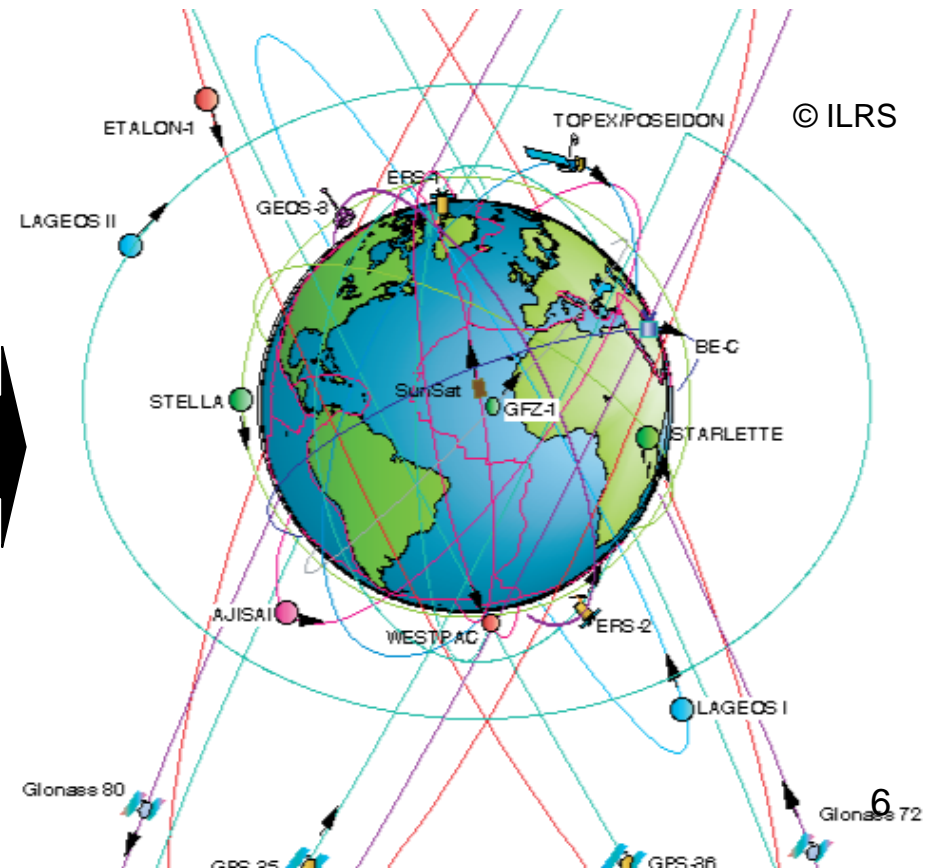
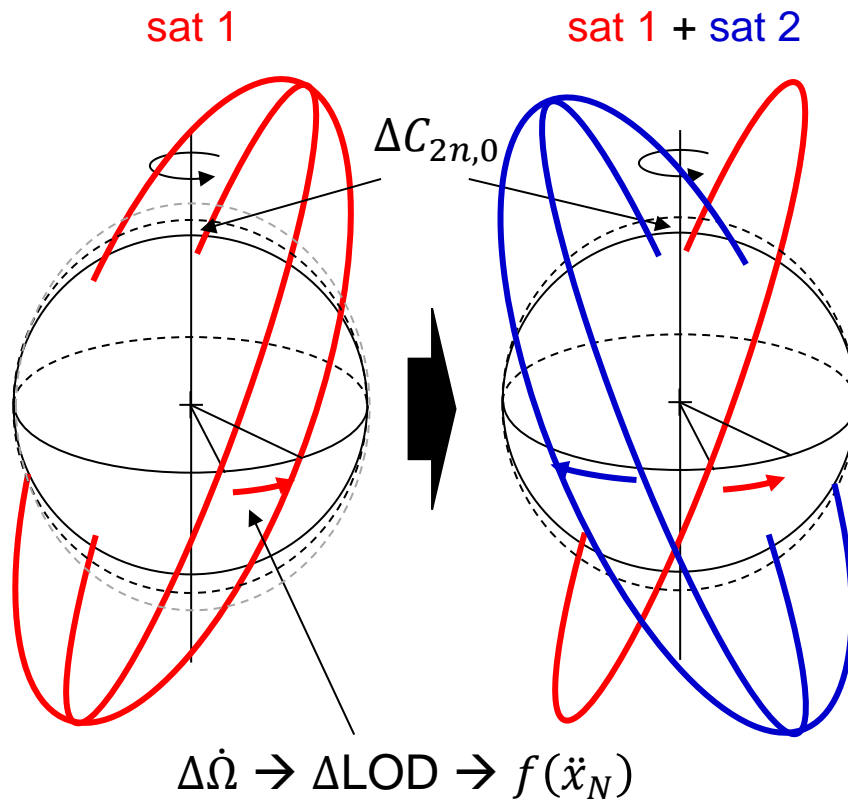
# Correlations II

- **sat 1**: high correlations between Earth gravity field, nodal precession, empirical cross-track accelerations and Earth rotation
- **sat 1** + **sat 2**: mixed inclinations are important to decorrelate Earth gravity field, satellite orbit and Earth rotation
- optimal mix would be the **butterfly configuration** ( $I_1 - 90^\circ = 90^\circ - I_2$ )  
→ precession of nodes in opposite direction with the same velocity



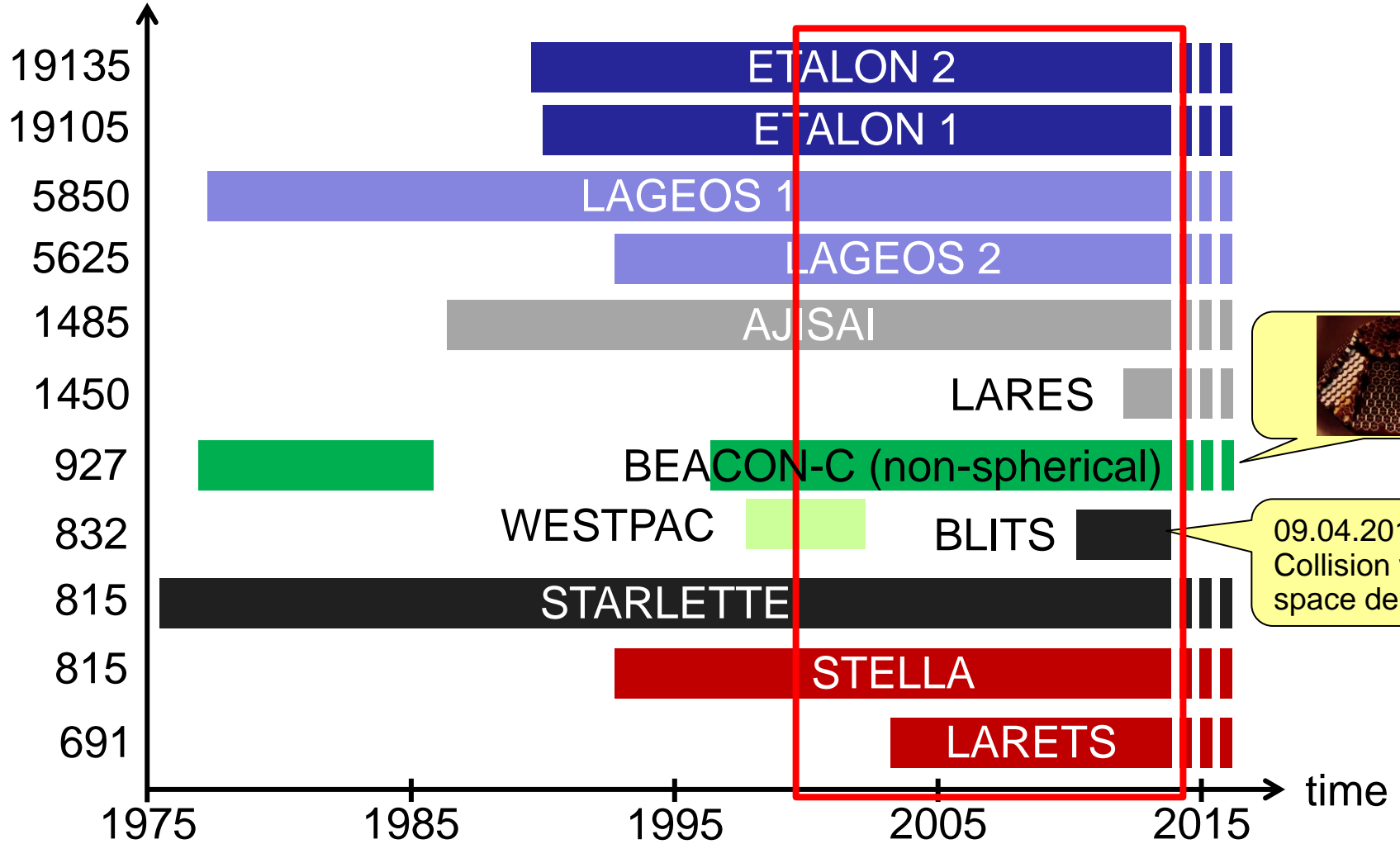
# Correlations III

- **sat 1**: high correlations between Earth gravity field, nodal precession, empirical cross-track accelerations and Earth rotation
- **sat 1 + sat 2**: mixed inclinations are important to decorrelate Earth gravity field, satellite orbit and Earth rotation
- optimal mix would be the **butterfly configuration** ( $I_1 - 90^\circ = 90^\circ - I_2$ )  
 → precession of nodes in opposite direction with the same velocity



# Data I

satellite altitude [km]



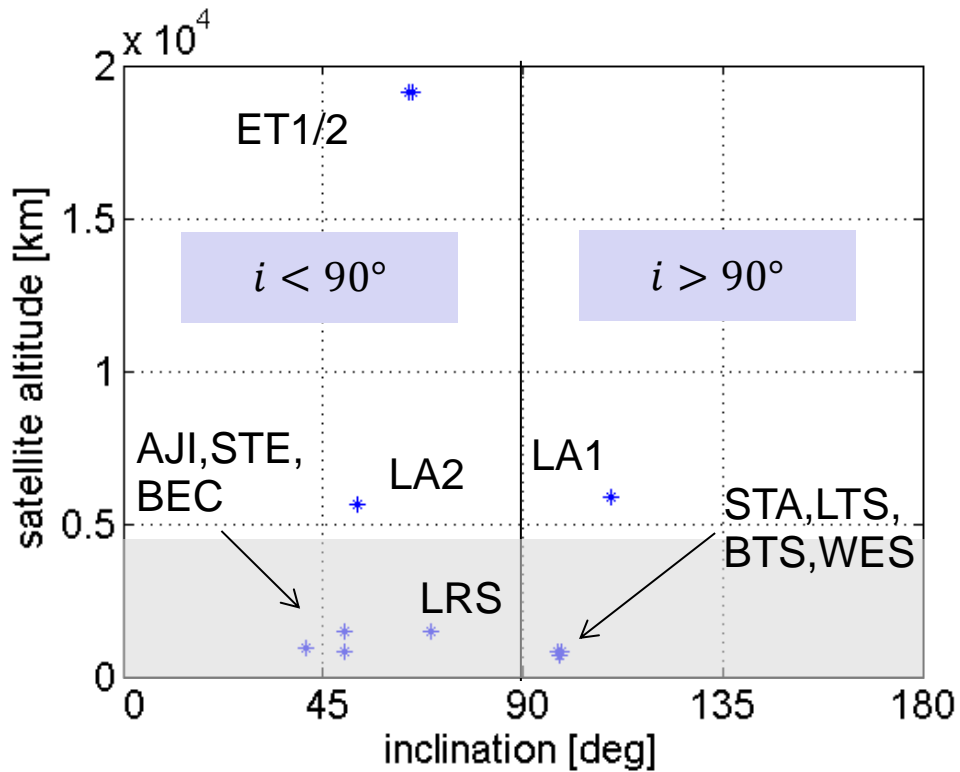
© ILRS

09.04.2013:  
Collision with  
space debris

not included yet

Computation period  
2000.0 until 2013.5

# Data II

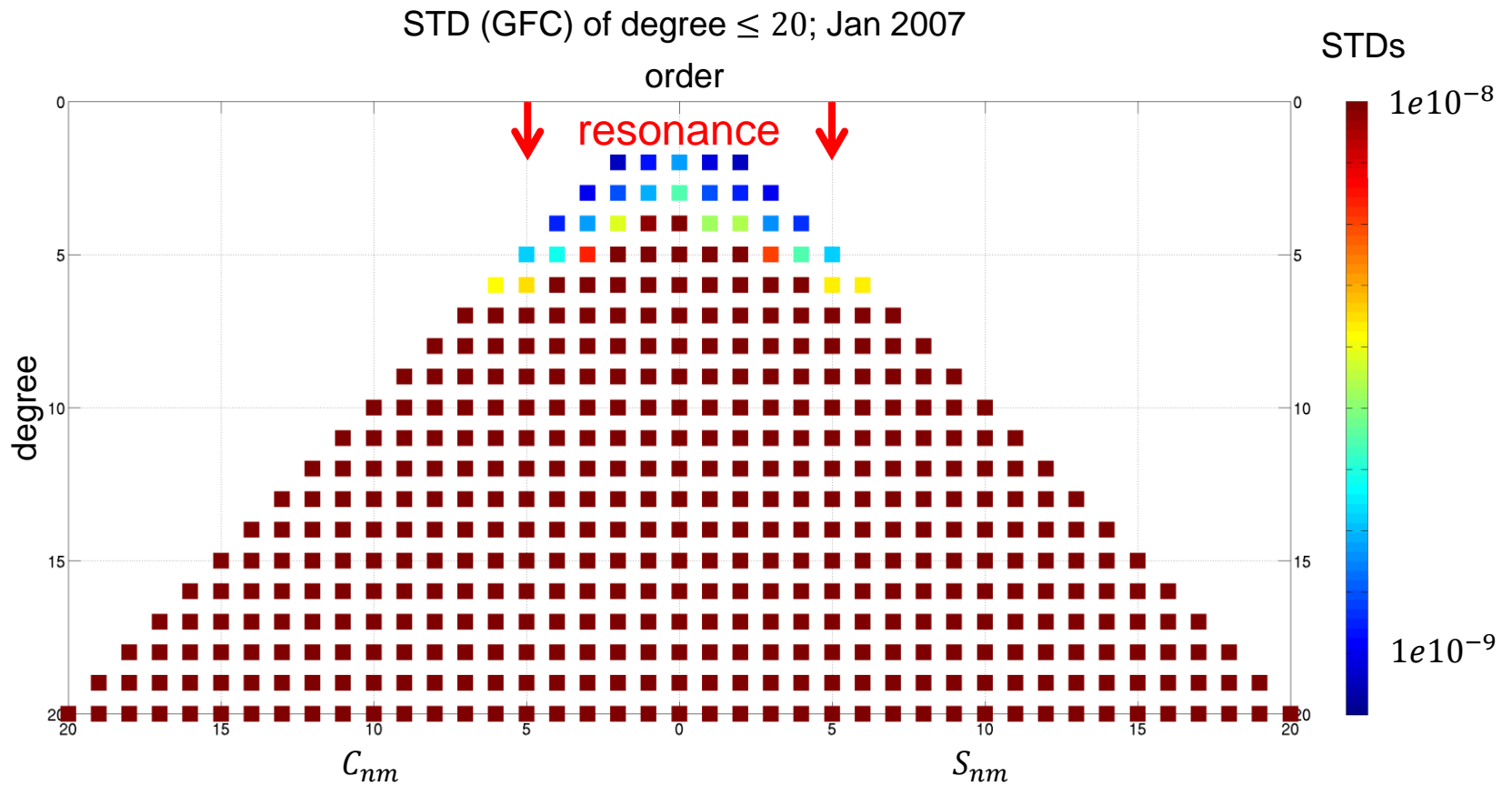


satellite	mass [kg]	diameter [m]	rev.-period [h]
LAGEOS1	406.97	0.60	3.76
LAGEOS2	405.38	0.60	3.76
ETALON1	1415.0	1.294	11.26
ETALON2	1415.0	1.294	11.26
STELLA	47.3	0.24	1.74
STARLETTE	47.0	0.24	1.69
AJISAI	685.0	2.15	1.93
LARETS	23.28	0.21	1.64
LARES	386.8	0.364	1.91
BLITS	7.53	0.17	1.68
BEACONC	52.6	non-sph.	1.80

- Observations are combined on the NEQ-level
- Weighting of NEQs is done via VCE
- LARETS, BLITS, BEACONC and STELLA get lower weights



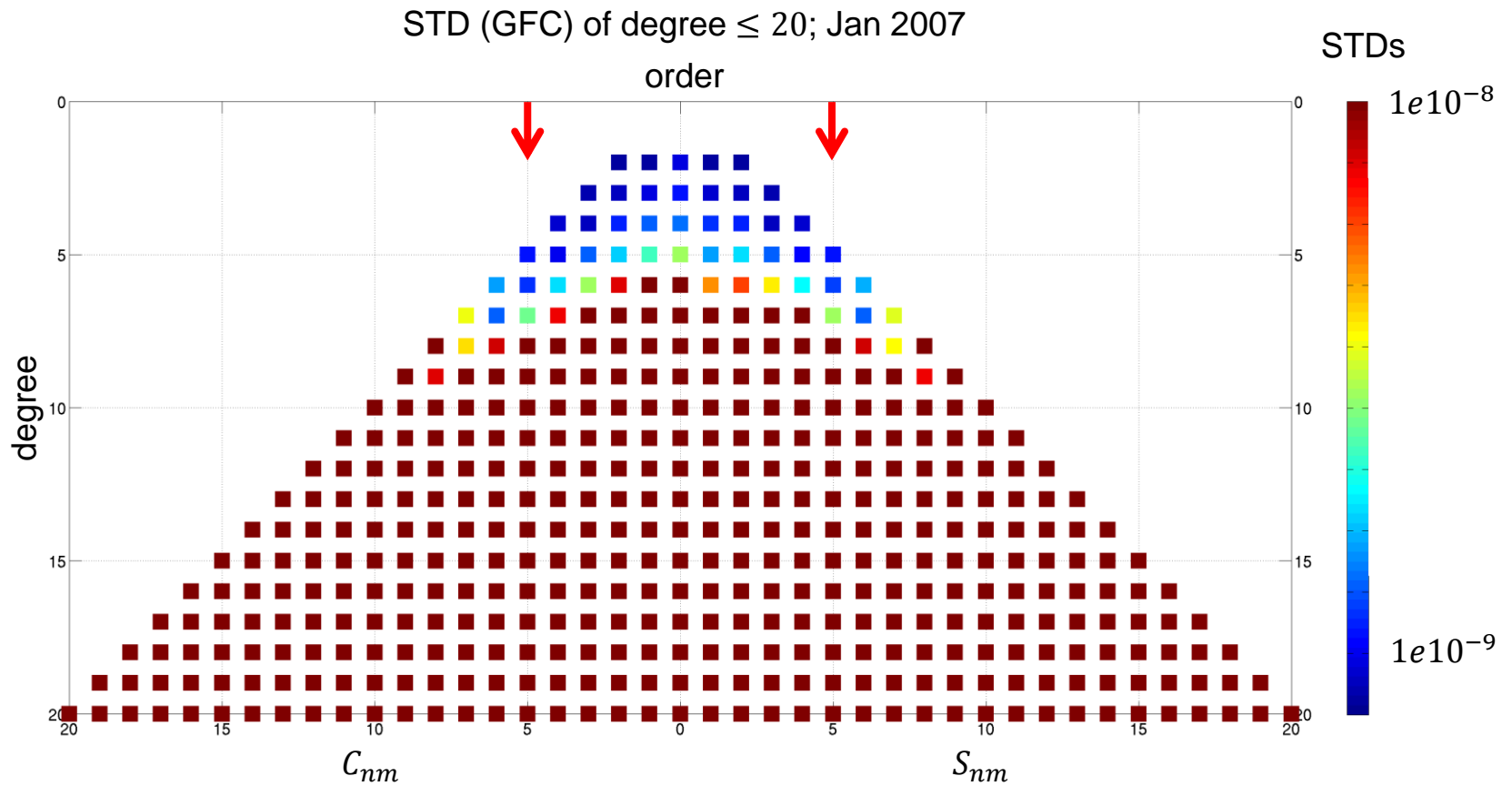
# Earth gravity field I



## LAGEOS1

- low sensitivity on GFCs of degree  $> 3$
- high correlations of low-degree GFCs with satellite orbit

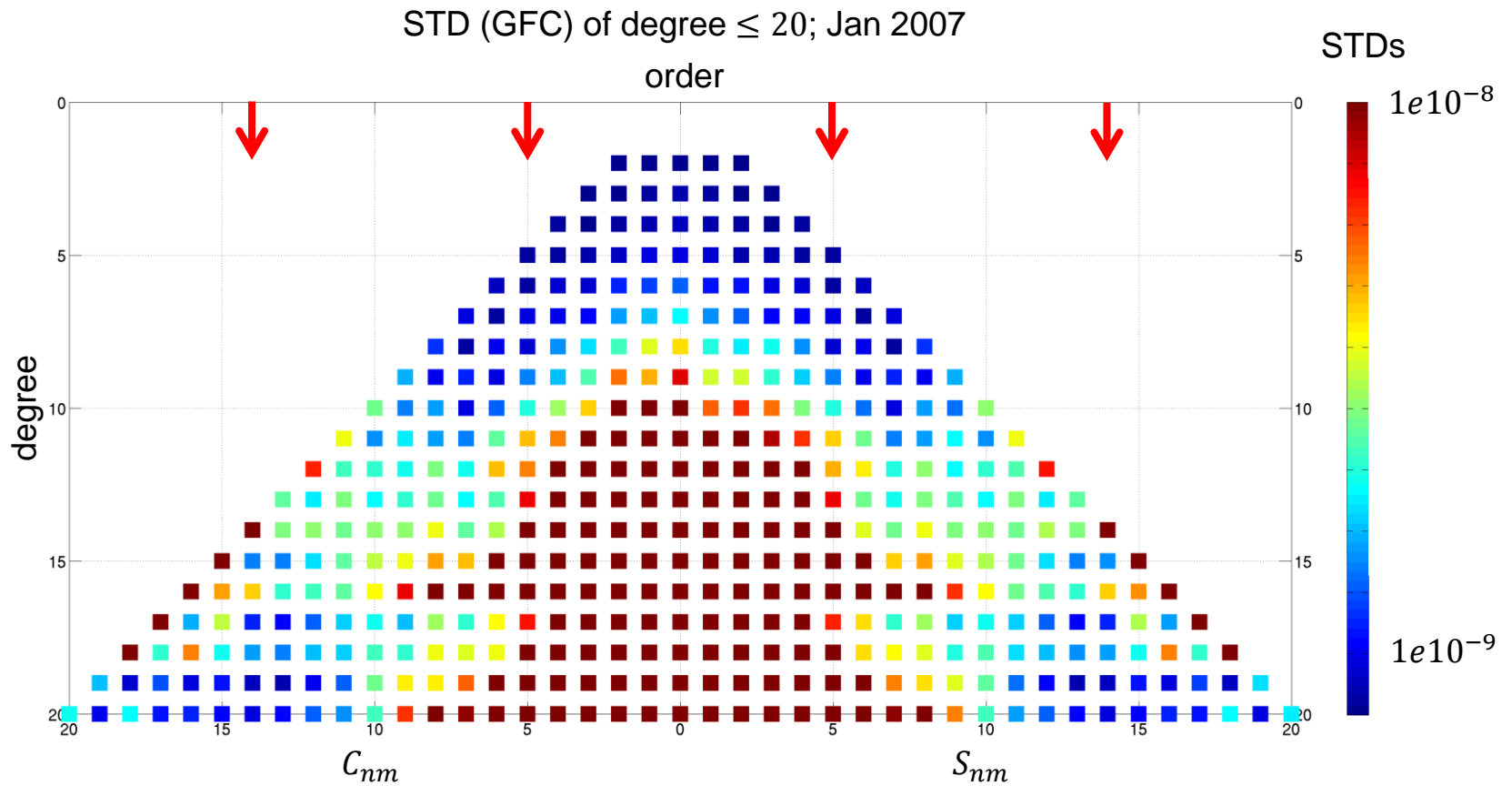
# Earth gravity field II



## LAGEOS1/2

- stable estimation of GFCs of degree  $\leq 4$
- decorrelation of low-degree GFCs with satellite orbits due to mixed inclinations

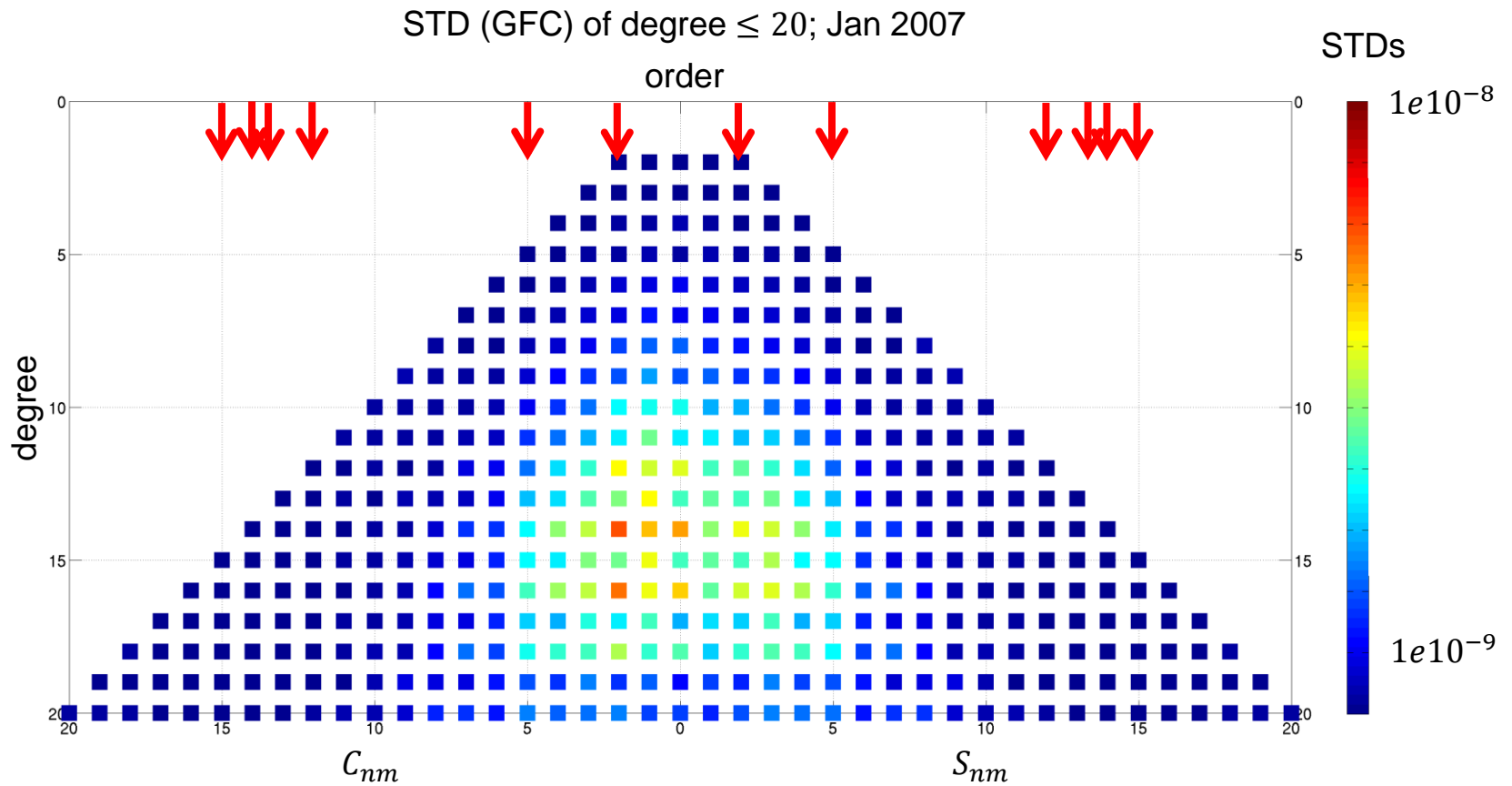
# Earth gravity field III



## LAGEOS1/2 + STARLETTE

- stable estimation of GFCs of degree  $\leq 6$
- decrease of STD of tesseral GFCs
- STARLETTE has slightly lower  $\lambda$  than LAGEOS1/2  $\rightarrow$  high impact on GFC estimation

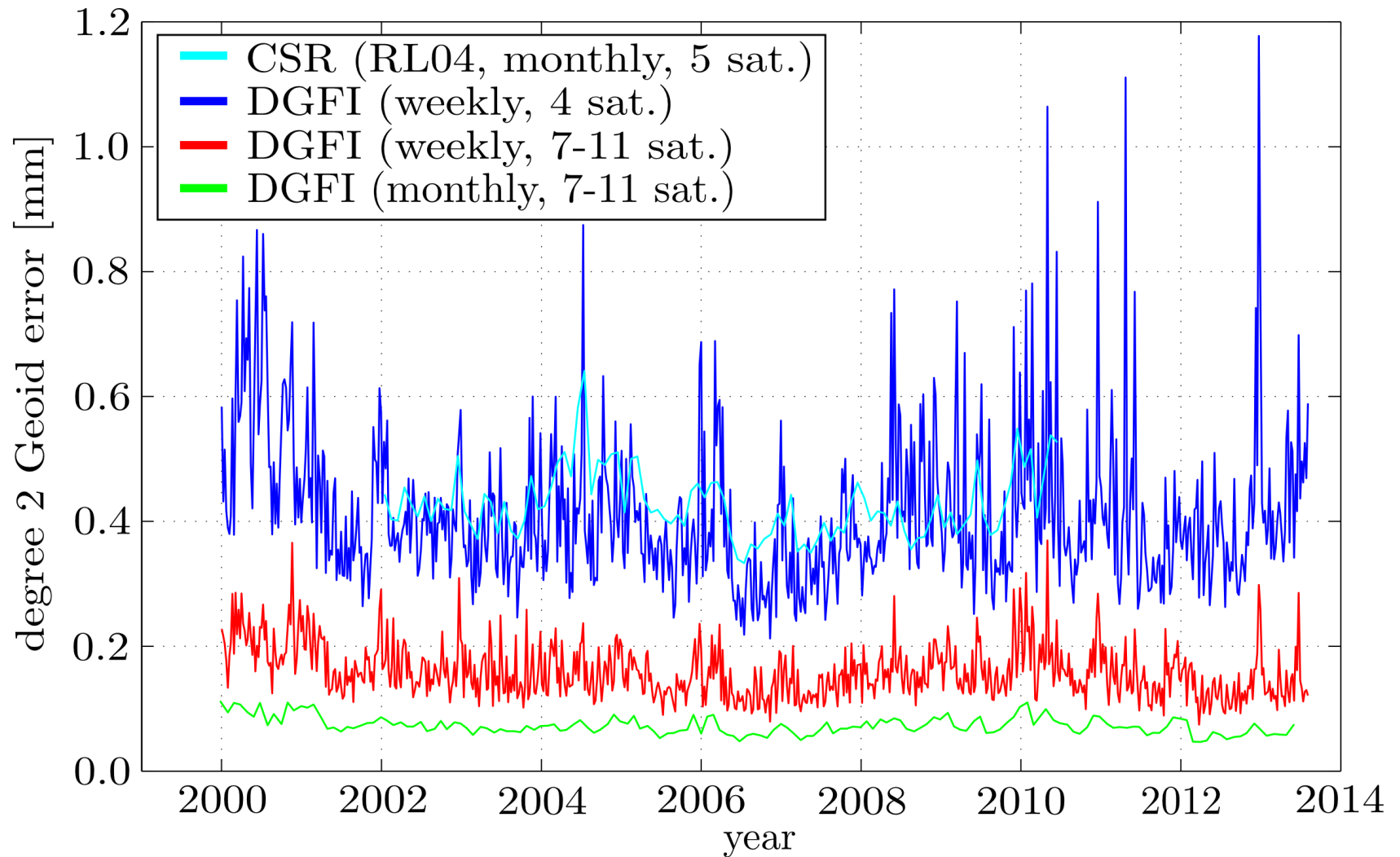
# Earth gravity field IV



## LAGEOS1/2 + ETALON1/2 + LARETS + STARLETTE + STELLA + AJISAI

- small STD of sectoral/tesseral GFCs up to degree  $\leq 20$
- zonal GFCs have higher STDs
- resonances of LEOs allow to estimate GFCs of high degree

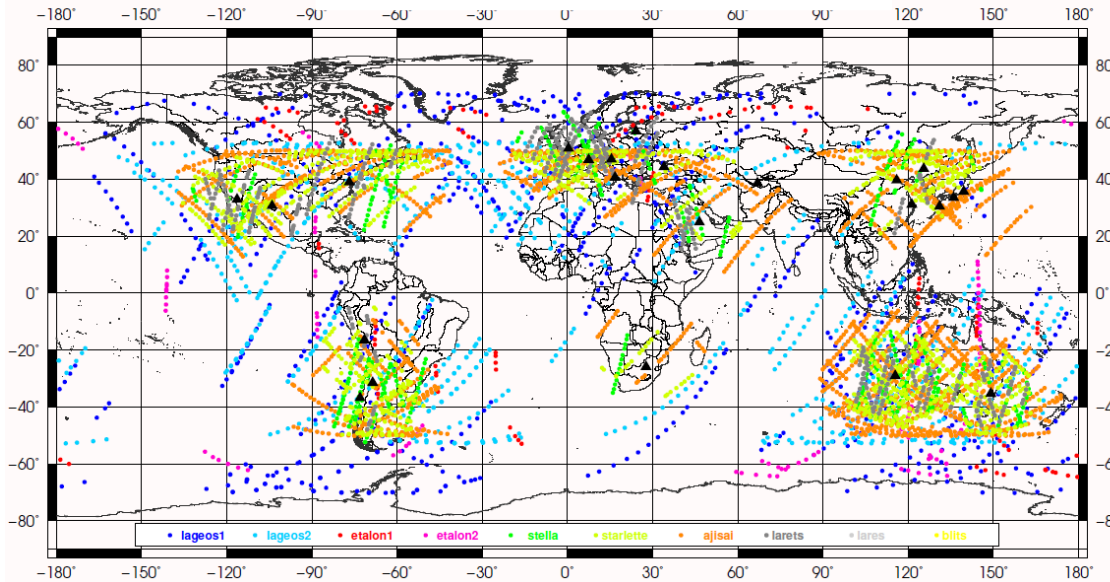
# Earth gravity field V



- weekly  $\sigma^2(c_2)$  of DGFI (11 sat.) is smaller than monthly  $\sigma^2(c_2)$  of CSR!

# weekly / monthly global observation coverage

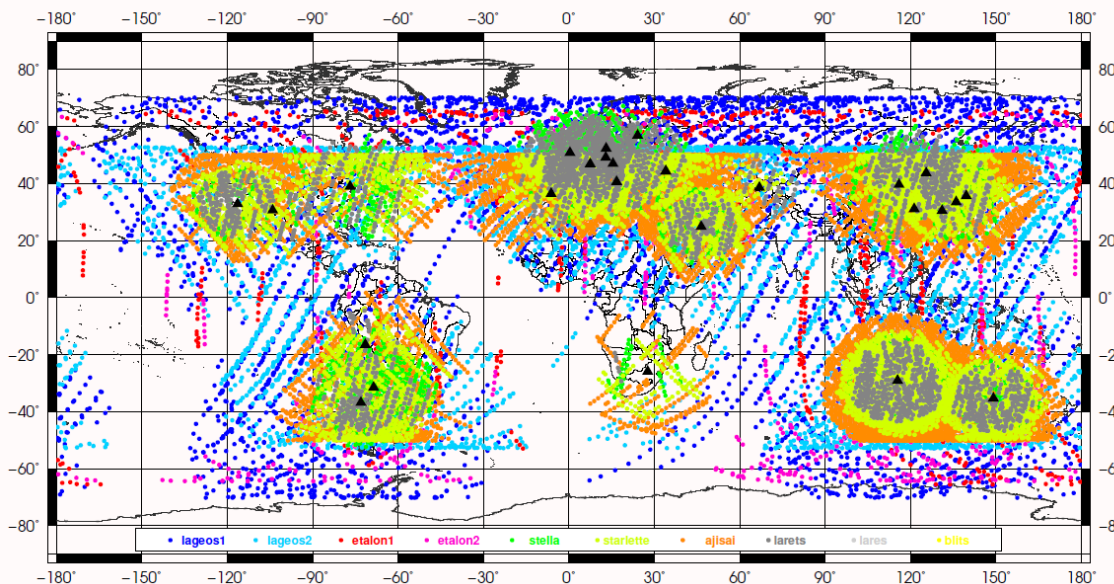
31.12.2006 – 07.01.2007



## weekly solution

- poor observation distribution
- sometimes bad observation geometry due to station outage
- high weekly variability

January 2007

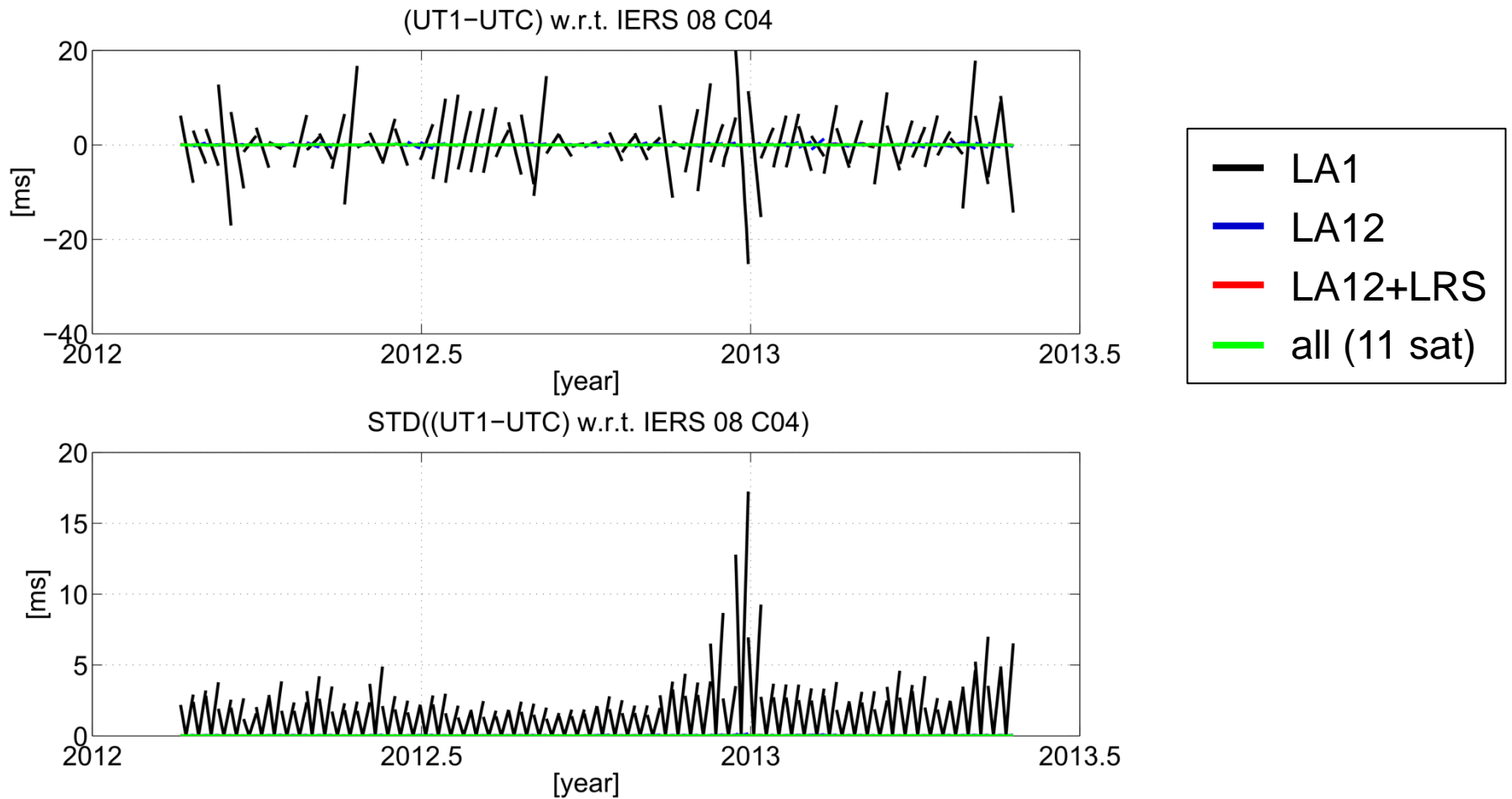


## monthly solution

- dense observation distribution
- good network geometry
- low monthly variability

# Earth Orientation Parameter I

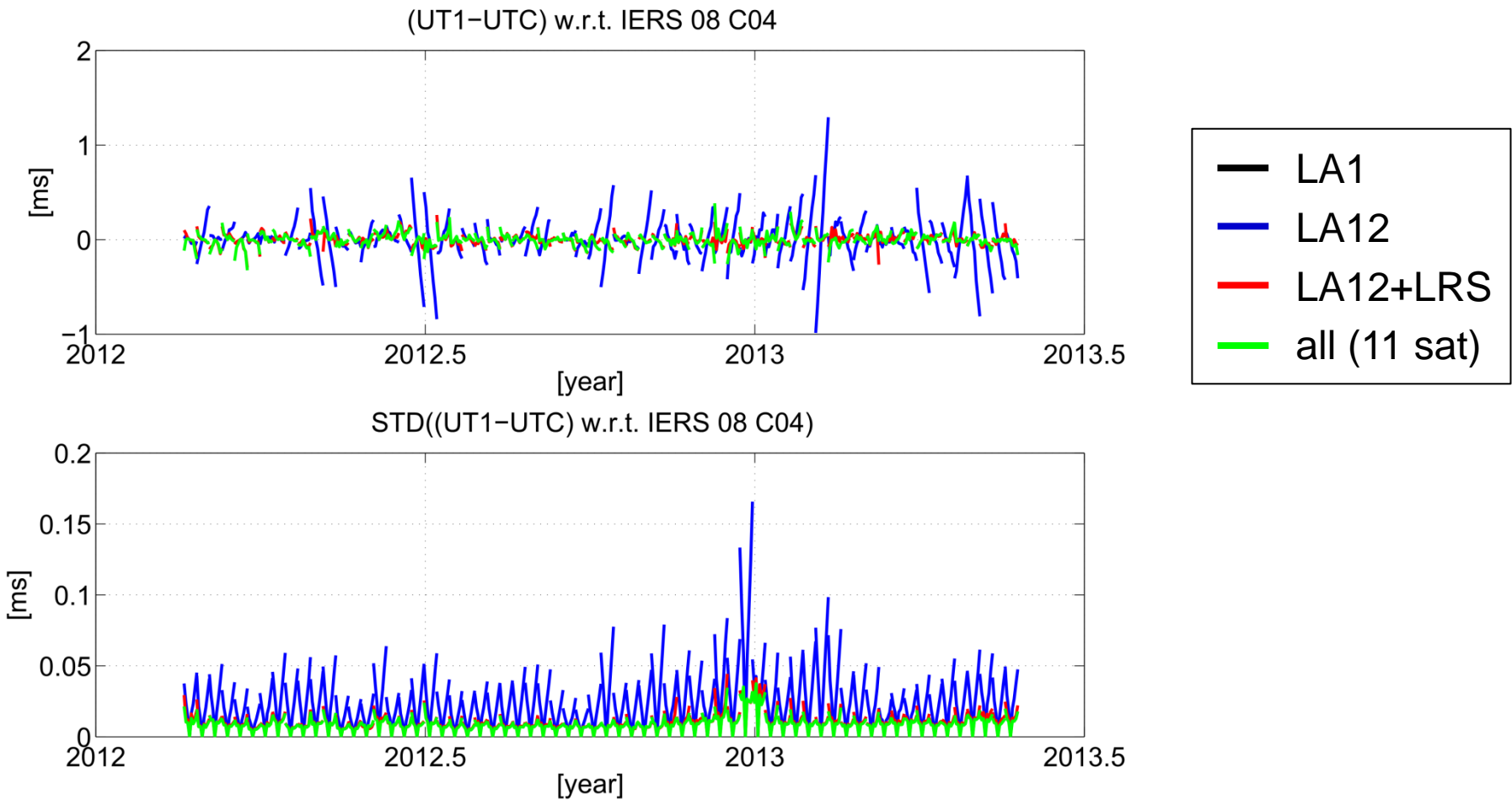
weekly solution between Feb. 2012 and May 2013 (LARES period)



<b>RMS <math>\Delta</math> x-pole [<math>\mu</math>as]</b>	39.2			
<b>RMS <math>\Delta</math> y-pole [<math>\mu</math>as]</b>	50.0			

# Earth Orientation Parameter II

weekly solution between Feb. 2012 and May 2013 (LARES period)

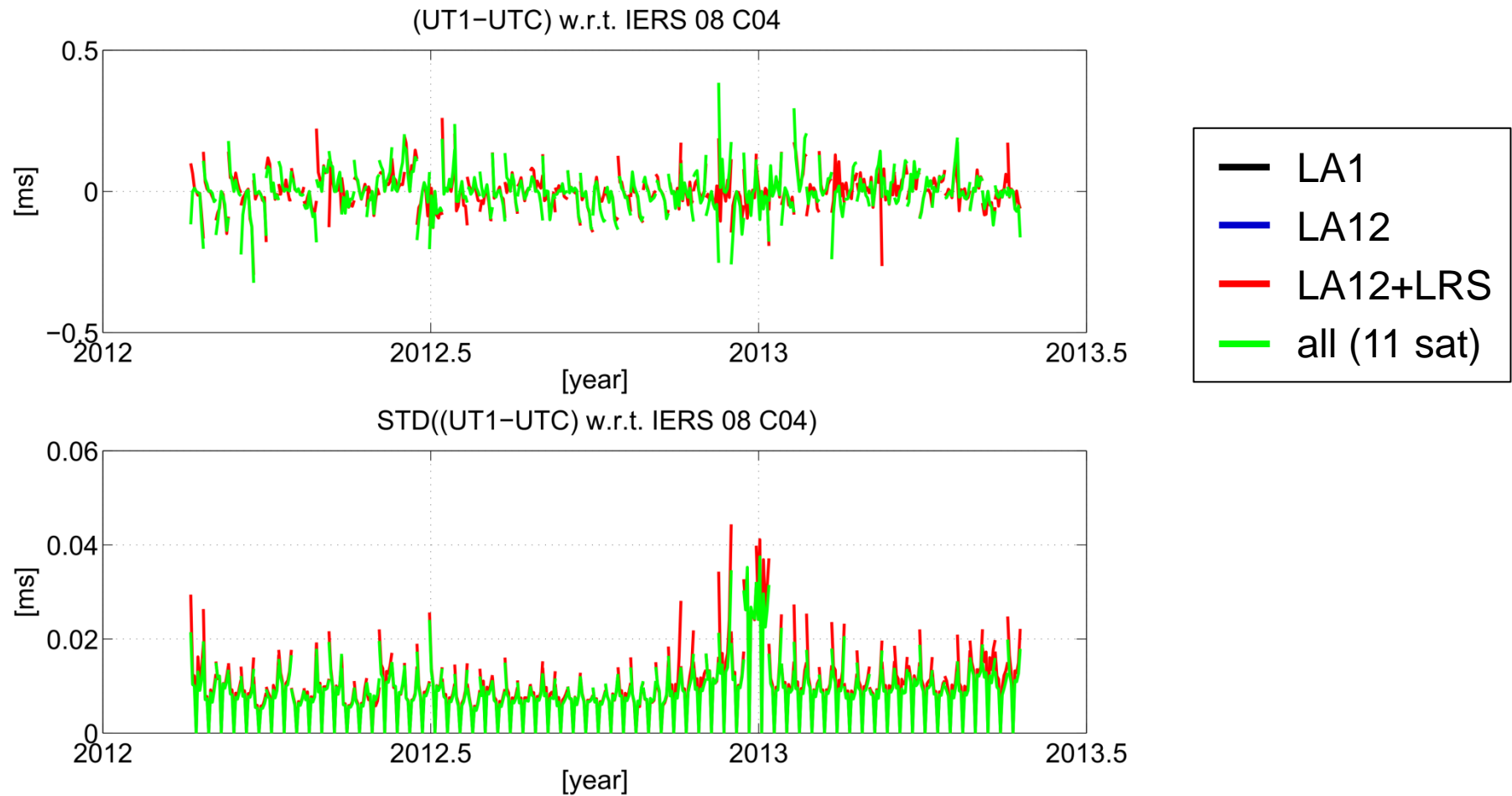


<b>RMS <math>\Delta</math> x-pole [<math>\mu</math>as]</b>	39.2	15.1		
<b>RMS <math>\Delta</math> y-pole [<math>\mu</math>as]</b>	50.0	16.1		



# Earth Orientation Parameter III

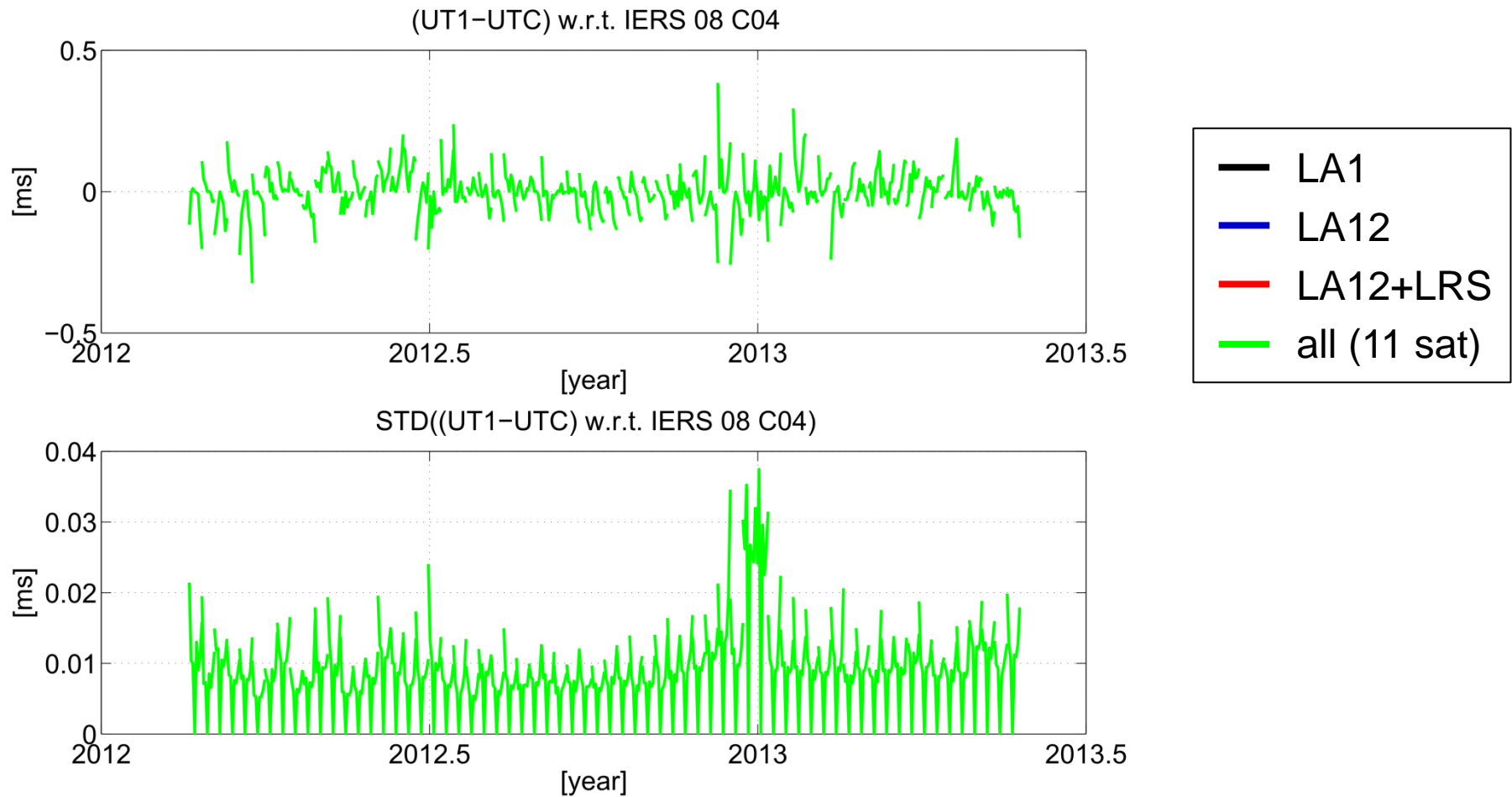
weekly solution between Feb. 2012 and May 2013 (LARES period)



<b>RMS <math>\Delta</math> x-pole [<math>\mu</math>as]</b>	39.2	15.1	15.3	
<b>RMS <math>\Delta</math> y-pole [<math>\mu</math>as]</b>	50.0	16.1	15.8	

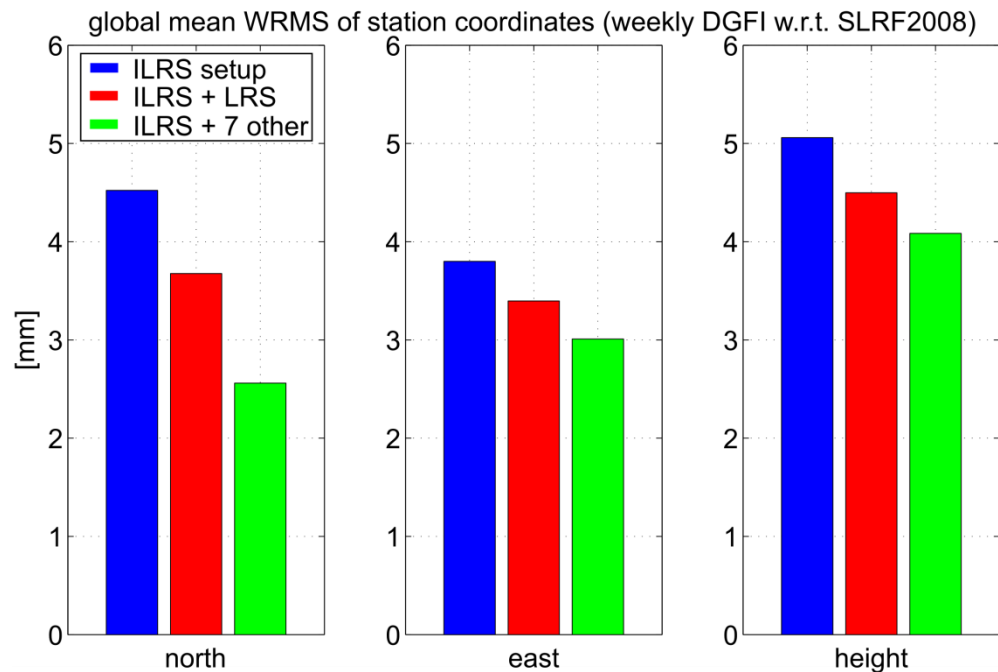
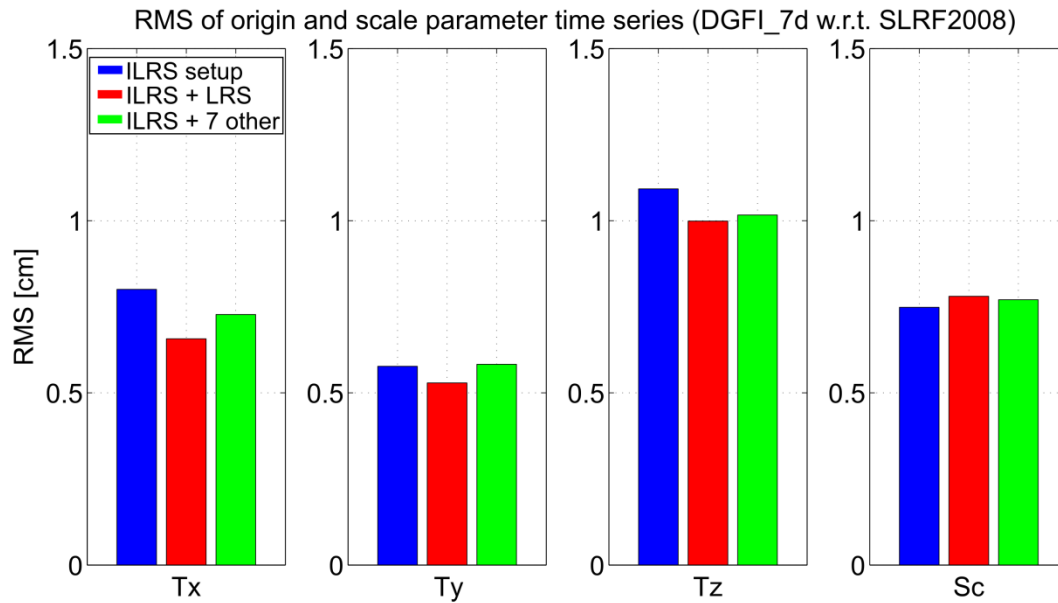
# Earth Orientation Parameter IV

weekly solution between Feb. 2012 and May 2013 (LARES period)



<b>RMS <math>\Delta</math> x-pole [<math>\mu</math>as]</b>	39.2	15.1	15.3	14.6
<b>RMS <math>\Delta</math> y-pole [<math>\mu</math>as]</b>	50.0	16.1	15.8	14.7

# Terrestrial Reference Frame



## RMS of translation / scale parameter w.r.t. SLRF2008

- Tx: -14 % (ILRS+LRS)  
- 7 % (11 sat)
- Ty: -6 % (ILRS+LRS)
- Tz: -7 % (ILRS+LRS)  
-6 % (11 sat)
- Sc: +4 % (ILRS+LRS)  
+3 % (11 sat)

## global mean coordinate WRMS

- north: -14 % (ILRS+LRS)  
-40 % (11 sat)
- east: -5 % (ILRS+LRS)  
-17 % (11 sat)
- height: -10 % (ILRS+LRS)  
-18 % (11 sat)

# Summary

- **Earth gravity field:**

- mix of different satellite heights and resonances allows to estimate stable GFCs together with orbit parameters, TRF and EOPs
- the longer the arc length is, the smaller are the STDs of the estimated GFCs (well-determined GFCs up to d/o 20 with monthly (4 weeks stacked) solutions!)

- **EOP:**

- mix of different satellite inclinations allows to reduce the (UT1-UTC) systematics (decorrelation of gravity, orbit and  $\Delta\text{LOD}$ )
- The more satellites are combined, the smaller is the scatter of the pole coordinates

- **TRF:**

- LARES helps to reduce the scatter of the transformation parameters & the global WRMS of the coordinates
- with 11 satellites, the global WRMS is reduced by about 20-40 % w.r.t. the ILRS (LA1/2, ET1/2) solution

Bloßfeld M., Müller H., Gerstl M., Stefka V., Bouman J. (2013)  
*Improved monthly Earth's gravity field solutions using multi-satellite SLR,*  
J Geophys Res, submitted soon

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<sup>2</sup>Astronomical Institute, Academy of Sciences of the Czech Republic  
email: [blossfeld@dgfi.badw.de](mailto:blossfeld@dgfi.badw.de)



# Relative weighting of satellites

- relative weighting using a variance component estimation (VCE) based on normal equations

$$N_c = \lambda_1 N_1 + \lambda_2 N_2 + \dots + \lambda_{10} N_{10} \quad \text{with} \quad \lambda_i = \frac{1}{\sigma_i^2}$$

satellite	$\sigma_0^2$ (TRF+EOP+GFC)
LA1	3.8
LA2	2.2
ET1	8.6
ET2	7.0
STE	34.6
STA	13.3
AJI	12.9
LTS	46.2
LRS	12.9
BTS	52.2
BEC	163.0

- Estimation of TRF+EOP+GFC in one combined adjustment
- STE: sun-synchronous orbit
- LTS: very poor AMR
- BTS: new reflector type, low weight
- BEC: non-spherical shape appr. With spherical model